

$$F(s) = \frac{s^2+1}{s(s+1)(s-2)}$$

$$f(t) = ?$$

$$F(s) = \frac{A_1}{(s+1)} + \frac{A_2}{(s-2)} + \frac{B}{s}$$

$$f(t) = A_1 \cdot e^{-t} + A_2 \cdot e^{2t} + B \cdot 1(t)$$

$$A_1 = \frac{(s^2+1) \cdot (\cancel{s+1})}{s \cdot (s+1) \cdot (s-2)} \Big|_{s=-1} = \frac{(-1)^2+1}{-1 \cdot (-1-2)} = \frac{2}{-1 \cdot (-3)} = \frac{2}{3}$$

$$A_2 = \frac{(s^2+1) \cdot (\cancel{s-2})}{s \cdot (s+1) \cdot (s-2)} \Big|_{s=2} = \frac{2^2+1}{2 \cdot (2+1)} = \frac{5}{6}$$

$$B = \frac{(s^2+1) \cdot \cancel{s}}{s \cdot (s+1) \cdot (s-2)} \Big|_{s=0} = \frac{0+1}{(0+1)(0-2)} = \frac{1}{-2} = -\frac{1}{2}$$

$$f(t) = \frac{2}{3} \cdot e^{-t} + \frac{5}{6} \cdot e^{2t} - \frac{1}{2} \cdot 1(t)$$